

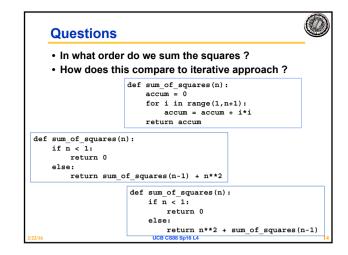
	In words	Q
	 The sum of no numbers is zero The sum of 1² through n² is the sum of 1² through (n-1)² plus n² 	
(<pre>def sum_of_squares(n): if n < 1:</pre>	
	return 0	
	else:	
	return sum_of_squares(n-1) + n**2	

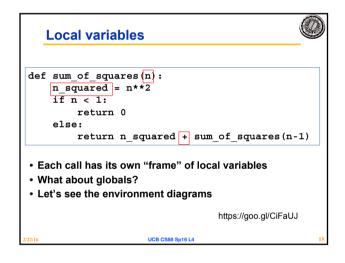
Why d	oes it work	Ø					
<pre>sum_of_squares(3)</pre>							
# sum_of_sq # # #	uares(3) => sum_of_squares(2) + 3**2 => sum_of_squares(1) + 2**2 + 3**2 => sum_of_squares(0) + 1**2 + 2**2 + => 0 + 1**2 + 2**2 + 3**2 = 14	- 3**2					
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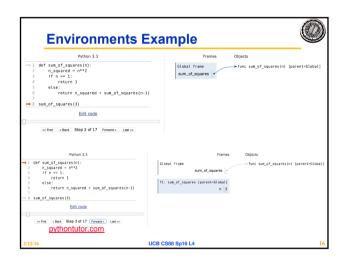
How does it work?

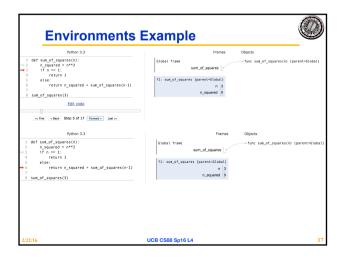
- Each recursive call gets its own local variables
 Just like any other function call
- Computes its result (possibly using additional calls)
- Just like any other function call
 Returns its result and returns control to its caller
- Just like any other function call
- The function that is called happens to be itself
 – Called on a simpler problem
 - Eventually bottoms out on the simple base case
- · Reason about correctness "by induction"
 - Solve a base case
 - Assuming a solution to a smaller problem, extend it

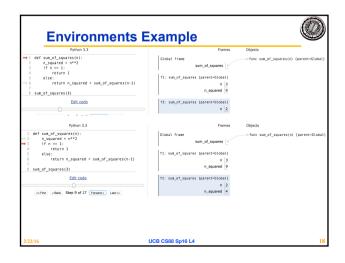
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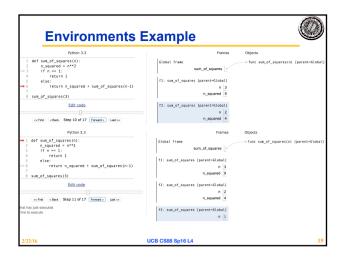












Environments E	xample	Ø
Python 3.3	Frames	Objects
1 def sum_0f_squares(n): -2 n_squared = n**2 →3 if n == 1: 4 return 1 5 else: 6 return n_squared + sum_of_squares(n-1) 7 8 sum of squares(3)	Global frame sum_of_squares [f1: sum_of_squares (parent=Global) n [3] n_squared [9]	⇒func sum_of_squares(n) [parent=Global]
Edit code	f2: sum_of_squares [parent=Global] n 2 n_squared 4 f3: sum_of_squares [parent=Global] n_squared 1	
Python 3.3	Frames	Objects
1 def sum_of_squares(n): 2 n_squared = n**2 →3 if n == 1: →4 return 1 5 else:	Global frame sum_of_squares [f1: sum_of_squares [parent=Global]	<pre>>> func sum_of_squares(n) [parent=Global]</pre>
<pre>6 return n_squared + sum_of_squares(n-1) 7 8 sum_of_squares(3)</pre>	n 3 n_squared 9	
Edit.code	f2: sum_of_squares [parent=Global] n 2 n_squared 4	
that has just executed : The to execute	f3: sum_of_squares [parent=Global] n 1 n_squared 1	

