



UC Berkeley EECS
Lecturer
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Computational Structures in Data Science



Lists & Higher Order Functions



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Functions That Make Functions



Learning Objectives

- Learn how to use and create higher order functions:
- Functions can be used as data
- Functions can accept a function as an argument
- **Functions can return a new function**



Review: What is a Higher Order Function?

- A function that takes in another function as an argument

OR

- A function that returns a function as a result.



Higher Order Functions

- **A function that returns (makes) a function**

```
def leq_maker(c):  
    def leq(val):  
        return val <= c  
    return leq
```

```
>>> leq_maker(3)  
<function leq_maker.<locals>.leq at 0x1019d8c80>
```

```
>>> leq_maker(3)(4)  
False
```

```
>>> [x for x in range(7) if leq_maker(3)(x)]  
[0, 1, 2, 3]
```

Demo



- [PythonTutor Link](#)



Learning Objectives

- Learn three new common Higher Order Functions:
 - map, filter, reduce
- These each apply a function to a sequence (list) of data
- They are “lazy” so we may need to call `list()`

- Map: Transform each item
 - Input: A function and a sequence
 - Output: A sequence of the same length. The items may be different.



Functional List Operations

- Goal: Transform a list, and return a new result
- We'll use 3 functions that are hallmarks of functional programming
- Each of these takes in a function and a sequence

Function Name	Action	Input arguments	Input Fn. Returns	Output List
map	Transform every item	1 argument (each item)	"Anything", a new item	List of the same length, but possibly new values
filter	Return a list with fewer items	1 argument (each item)	A Boolean	List with possibly fewer items, but values are the same
reduce	"Combine" items together	2 arguments (current item, and the previous result)	Type should match the type each item	Usually a "single" item

MAP



```
list(map(function_to_apply, list_of_inputs))
```

Transform each of items by a function.

e.g. `square()`

Inputs (Domain):

- Function
- Sequence

Output (Range):

- A sequence

```
def map(function, sequence):  
    return [ function(item) for item in sequence ]
```

```
list(map(square, range(10)))
```



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Lists & Higher Order Functions: Filter



Learning Objectives

- Learn three new common Higher Order Functions:
 - map, filter, reduce
- These each apply a function to a sequence (list) of data
- map/filter are “lazy” so we may need to call `list()`

- Filter: Keeps items matching a condition.
 - Input: A function and sequence
 - Output: A sequence, possibly with items removed. The items don’t change.



FILTER

```
list(filter(function, list_of_inputs))
```

Keeps each of item where the function is true.

Inputs (Domain):

- Function
- Sequence

Output (Range):

- A sequence

```
def filter(function, sequence):  
    return [ item for item in sequence if function(item) ]
```



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Lists & Higher Order Functions Reduce



Learning Objectives

- Learn three new common Higher Order Functions:
 - map, filter, reduce
- These each apply a function to a sequence (list) of data
- Reduce: “Combines” items together, probably doesn’t return a list.
 - Input: A 2 item function and a sequence
 - A single value

REDUCE



```
reduce(function, list_of_inputs)
```

Successively **combine** items of our sequence

- function: add(), takes 2 inputs gives us 1 value.

Inputs (Domain):

- Function, with 2 inputs
- Sequence

Output (Range):

- An item, the type is the output of our function.

Note: We must import reduce from functools!

```
def reduce(function, sequence):  
    result = function(sequence[0], sequence[1])  
    for index in range(2, len(sequence)):  
        result = function(result, sequence[index])  
    return result
```



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Lists & Higher Order Functions Acronym



Today's Task: Acronym

Input: "The University of California at Berkeley"

Output: "UCB"

```
def acronym(sentence):  
    """YOUR CODE HERE"""
```

P.S. Pedantry alert: This is really an *initialism* but that's rather annoying to say and type. ☺ (However, the code we write is the same, the difference is in how you pronounce the result.) The more you know!



Three super important HOFs

* For the builtin filter/map, you need to then call list on it to get a list.

If we define our own, we do not need to call list

```
list(map(function_to_apply, list_of_inputs))
```

Applies function to each element of the list

```
list(filter(condition, list_of_inputs))
```

Returns a list of elements for which the condition is true

```
reduce(function, list_of_inputs)
```

Applies the function, combining items of the list into a "single" value.



Functional List Operations

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