## DATA C88C

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# **1** Higher Order Functions

A **higher order function** (HOF) is a function that manipulates other functions by taking in functions as arguments, returning a function, or both.

### 1.1 Functions as Arguments

One way a higher order function can exploit other functions is by taking functions as input. Consider this higher order function called negate.

def negate(f, x):
 return -f(x)

negate takes in a function f and a number x. It doesn't care what exactly f does, as long as f takes in a number and returns a number. Its job is simple: call f on x and return the negation of that value.

### 1.2 Questions

```
1. Here are some possible functions that can be passed through as f.
def square(n):
    return n * n

def double(n):
    return 2 * n

What will the following Python statements output?
>>> negate(square, 5)
>>> negate(double, -19)
```

```
>>> negate(double, negate(square, -4))
```

2. Implement a function keep\_ints, which takes in a function cond and a number n, and only prints a number from 1 to n if calling cond on that number returns True:

#### 1.3 Functions as Return Values

Often, we will need to write a function that returns another function. One way to do this is to define a function inside of a function:

```
def outer(x):
    def inner(y):
        ...
    return inner
```

The return value of outer is the function inner. This is a case of a function returning a function. In this example, inner is defined inside of outer. Although this is a common pattern, we can also define inner outside of outer and still use the same return statement.

```
def inner(y):
    ...
def outer(x):
    return inner
```

#### 1.4 Questions

1. Use this definition of outer to fill in what Python would print when the following lines are evaluated.

```
def outer(n):
    def inner(m):
        return n - m
    return inner
>>> outer(61)
>>> f = outer(10)
>>> f(4)
>>> outer(5)(4)
```

DISCUSSION 3: HIGHER ORDER FUNCTIONS

2. Implement a function keep\_ints like before, but now it takes in a number n and returns a function that has one parameter cond. The returned function prints out all numbers from 1..i..n where calling cond(i) returns True.

```
def keep_ints(n):
    """Returns a function which takes one parameter cond and
    prints out all integers 1..i..n where calling cond(i)
    returns True.
    >>> def is_even(x):
        ...  # Even numbers have remainder 0 when divided by 2.
        ...  return x % 2 == 0
    >>> keep_ints(5)(is_even)
    2
    4
    """
```

# 2 Environment Diagrams

1. Draw the environment diagram for evaluating the following code.

def f(x):
 return y + x
y = 10
f(8)

2. Draw the environment diagram for evaluating the following code.

DISCUSSION 3: HIGHER ORDER FUNCTIONS

```
3. Draw the environment diagram for evaluating the following code.
def foo(x, y):
    foo = bar
    return foo(bar(x, x), y)

def bar(z, x):
    return z + y

y = 5
foo(1, 2)
```