

- 1.Create a new local frame with the same parent as the function that was applied.
- 2.Bind the arguments to the function's formal parameter names in that frame.
- 3. Execute the body of the function in the environment beginning at that frame.

Execution rule for def statements:

- 1.Create a new function value with the specified name, formal
- parameters, and function body. Its parent is the first frame of the current environment.
- 3.Bind the name of the function to the function value in the first frame of the current environment.

Execution rule for assignment statements:

1.Evaluate the expression(s) on the right of the equal sign. 2.Simultaneously bind the names on the left to those values, in the first frame of the current environment.

Execution rule for conditional statements:

Each clause is considered in order. 1. Evaluate the header's expression.

2.If it is a true value, execute the suite, then skip the remaining clauses in the statement.

Evaluation rule for or expressions:

- 1. Evaluate the subexpression <left>.
- 2.If the result is a true value $\boldsymbol{v}\text{,}$ then the expression evaluates to v.
- 3.Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for and expressions:

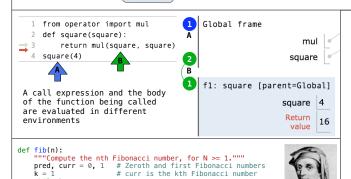
- 1. Evaluate the subexpression <left>.
- 2.If the result is a false value v, then the expression evaluates to v.
- 3.Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for not expressions:

1. Evaluate <exp>; The value is True if the result is a false value, and False otherwise.

Execution rule for while statements:

- 1. Evaluate the header's expression.
- If it is a true value, execute the (whole) suite, then return to step 1.



Function of a single argument (not called term) def cube(k): return pow(k, 3) A formal parameter that will def summation(n, term) be bound to a function """Sum the first n terms of a sequence. >>> summation(5, cube) 225 The cube function is passed as an argument value total, k = 0, 1 while k <= n:</pre> total, k = total + (term(k)), k + 1return total The function bound to term $0 + 1^3 + 2^3 + 3^3 + 4^3 + 5^5$ gets called here

return curr

Higher-or argument Nested de function def statements: Functions
on bodies are bound to nam rder val r **function:** lue or retu rns function a funct ion as defined a tak | within |e local kes a fu return funct n val other frame ue. as

names

Ħ.

the

> 2

1024

None

def abs_value(x):

else:

if x > 0:

return 0

return -x

return x elif x == 0:



```
Lists:
>>> digits = [1, 8, 2, 8]
>>> len(digits)
                digits ___
>>> digits[3]
                                  8 2 8
>>> [2, 7] + digits * 2
[2, 7, 1, 8, 2, 8, 1, 8, 2, 8]
>>> pairs = [[10, 20], [30, 40]]
>>> pairs[1]
                pairs
[30, 40]
                                    10 20
>>> pairs[1][0]
30
Executing a for statement:
for <name> in <expression>:
                                    30
                                         40
    <suite>
1. Evaluate the header <expression>
   which must yield an iterable value
   (a list, tuple, iterator, etc.)
 2. For each element in that sequence,
   in order:
  A. Bind <name> to that element in
     the current frame
  B. Execute the <suite>
 Unpacking in a
                      A sequence of
 for statement:
                   fixed-length sequences
>>> pairs=[[1, 2], [2, 2], [3, 2], [4, 4]]
>>> same_count = 0
      A name for each element in a fixed-length sequence
>>> for x, y in pairs:
    if x == y:
            same_count = same_count + 1
    ..., -3, -2, -1, 0, 1, 2, 3, 4, ...
             range(-2, 2)
 Length: ending value - starting value
 Element selection: starting value + index
 >>> list(range(-2, 2)) { List constructor
 [-2, -1, 0, 1]
 >>> list(range(4)) { Range with a 0 starting value
 [0, 1, 2, 3]
                           Slicing:
Membership:
>>> digits = [1, 8, 2, 8]
                           >>> digits[0:2]
                           [1, 8]
>>> 2 in digits
                           >>> digits[1:]
True
                           [8, 2, 8]
>>> 1828 not in digits
True
            Slicing creates a new object
Identity:
<exp0> is <exp1>
evaluates to True if both <exp0> and
<exp1> evaluate to the same object
Equality:
<exp0> == <exp1>
evaluates to True if both <exp0> and
<exp1> evaluate to equal values
Identical objects are always equal values
```

```
List comprehensions:
                                                                               List mutation:
   [<map exp> for <name> in <iter exp> if <filter exp>]
                                                                               >>> a = [10]
                                                                                                       >>> a = [10]
   Short version: [<map exp> for <name> in <iter exp>]
                                                                               >>> a == b
                                                                                                       >>> a == b
                                                                               True
                                                                                                       True
A combined expression that evaluates to a list using this
                                                                               >>> a.append(20)
                                                                                                       >>> b.append(20)
evaluation procedure:
                                                                               >>> a == b
                                                                                                       >>> a
1. Add a new frame with the current frame as its parent
                                                                               True
                                                                                                       [10]
2. Create an empty result list that is the value of the
                                                                                                       >>> b
                                                                               >>> a
                                                                               [10, 20]
                                                                                                       [10, 20]
3. For each element in the iterable value of <iter exp>:
                                                                                >>> b
                                                                                                       >>> a == b
   A. Bind <name> to that element in the new frame from step 1
                                                                               [10, 20]
                                                                                                       False
   B. If <filter exp> evaluates to a true value, then add
                                                                               You can {f copy} a list by calling the list constructor or slicing the list from the beginning to the end.
      the value of <map exp> to the result list
Dictionaries:
                                 Dictionary comprehensions:
                                                                               >>> a = [10, 20, 30]
                                                                                >>> list(a)
                                {key: value for <name> in <iter exp>}
         "más": "more",
"otro": "other",
                                                                               [10, 20, 30]
                                 >>> {x: x*x for x in range(3,6)}
                                                                                >>> a[:]
         "agua": "water"
                                 {3: 9, 4: 16, 5: 25}
                                                                               [10, 20, 30]
 }
                                                                                Tuples:
                                  >>> [word for word in words]
['más', 'otro', 'agua']
>>> [words[word] for word in words]
 >>> len(words)
                                                                                >>> empty = ()
  >>> "aqua" in words
                                                                                >>> len(empty)
                                 ['more', 'other', 'water']
>>> words["oruguita"] = 'caterpillar'
                                                                                0
  >>> words["otro"]
'other'
                                 >>> words["oruguita"]
'caterpillar'
>>> words["oruguita"] += '%'
                                                                                >>> conditions = ('rain', 'shine')
 >>> words["pavo"]
KeyError
                                                                                >>> conditions[0]
  >>> words.get("pavo", ";)'
                                 >>> words["oruguita"]
'caterpillar%'
                                                                                >>> conditions[0] = 'fog'
                                                                                Error
                                                                                >>> all([])
                                                                                                        >>> any([])
                                                                                >>> sum([1, 2])
                                                                                                        >>> max(1, 2)
                                                                                >>> sum([1, 2], 3)
                                                                                                        >>> max([1, 2])
                                                                                >>> sum([])
                                                                                                        >>> max([1, -2], key=abs)
                                                                                >>> sum([[1], [2]], [])
                                                                               List methods:
                                                                               >>> suits = ['coin', 'string', 'myriad']
                                                                               >>> suits.pop()
                                                                                                              Remove and return
                                                                               'mvriad'
                                                                               >>> suits.remove('string')
                                                                                                                Removes first
                                                                               >>> suits.append('cup')
>>> suits.extend(['sword', 'club'])
                                                                                                                matching value
                                                                               >>> suits[2] = 'spade'
                                                                               >>> suits
                                                                               ['coin',
def cascade(n):
                        >>> cascade(123)
                                                                               >>> suits
                                              virfib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21,
                                                                               >>> sults
['diamond', 'spade', 'club']
>>> suits.insert(0, 'heart')
Add an element
at an index
                        123
   if n < 10:
                                        def virfib(n):
        print(n)
                                          if n == 0:
return 0
elif n == 1
return 1
                                                                               >>> suits
        print(n)
                                                                               ['heart', 'diamond', 'spade', 'club']
        cascade(n//10)
        print(n)
                                                                               False values:
                                            return virfib(n-2) + virfib(n-1)
                                                                                                      >>> bool(0)
                                                                                Zero
                                                                                                      >>> hool (1)
                                                                               False
                                                                                                       True
                                                                               None
                                                                                                       >>> bool(''')
                                                                               •An empty string,
                                                                                                       False
                                                                                list, dict, tuple
                                                                                                      >>> bool('0')
                                                                                                       True
>>> bool([])
                                                                               All other values
                                                                                                       False
                                                                               are true values.
                                                                                                       >>> bool([[]])
                                                                                                      True >>> bool({})
                                                                                                      False
                                                                                                       >>> bool(())
                                                                                                      False
                                                                                                       >>> bool(lambda x: 0)
                                                                                                      True
                                                                               > func make withdraw list(balance) [parent=Global]
                               Global frame
                                                  make_withdraw_list
                                                                                          It changes the contents
                                                           withdraw •
                                                                                               of the b list
                                                                                 75
                               f1: make_withdraw_list [parent=Global]
                                                                               func withdraw(amount) [parent=f1]
                                                          balance 100
                                        withdraw
                                                                                          __def make_withdraw_list(balance):
                                                         withdraw
                                        doesn't
                                                                                              - b = [balance]
                                                                             Name bound
                                                               b
                                      reassign any
                                                                                               def withdraw(amount):
                                                                             outside of
                                                                                                 if amount > b[0]:
                                      name within
                                                            Return
                                                                            withdraw def
                                                                                                      return 'Insufficient funds'
```

the parent

f2: withdraw [parent=f1]

b[0] = b[0] - amount return b[0]

ithdraw = make_withdraw_list(100)

return withdraw

withdraw(25)

assignment

changes a list

amount 25

Return value 75





```
class Link:
                          Some zero
     empty = () < length sequence</pre>
                                                                 Link instance
                                                                                    Link instance
             _init__(self, first, rest=empty):
                                                                  first:
                                                                            4
                                                                                              5
                                                                                     first:
           self.first = first
           self.rest = rest
                                                                  rest:
                                                                                     rest:
              repr__(self):
                                                                >>> s = Link(4, Link(5))
           if self.rest:
                                                                 >>> 5
                rest = ', ' + repr(self.rest)
                                                                Link(4, Link(5))
           else:
                                                                 >>> s.first
                rest = ''
           return 'Link('+repr(self.first)+rest+
                                                                 >>> s.rest
                                                                Link(5
                                                                >>> print(s)
             _str__(self):
           string = '<
                                                                >>> print(s.rest)
           while self.rest is not Link.empty:
                                                                <5>
                string += str(self.first) +
self = self.rest
                                                                 >>> s.rest.rest is Link.empty
                                                                True
           return string + str(self.first) + '>'
                                                         def sum_digits(n):
    "-- +he digits of positive integer n."
Anatomy of a recursive function:

    The def statement header is like any function
    Conditional statements check for base cases
    Base cases are evaluated without recursive calls
    Recursive cases are evaluated with recursive calls

                                                              all_but_last, last = n // 10, n % 10
                                                              return sum digits(all but last) + last
Recursive decomposition: finding
                                            def count_partitions(n, m):
simpler instances of a problem.
E.g., count_partitions(6, 4)
                                                 if n == 0:
                                                      return 1
Explore two possibilities:
•Use at least one 4
                                                  elif n < 0:
                                                      return 0
                                                 elif m == 0:
*Don't use any 4
Solve two simpler problems:
                                                       return 0
count_partitions(2, 4)count_partitions(6, 3)
                                                 else:
                                                   with m = count partitions(n-m, m)
Tree recursion often involves
                                                      without_m = count_partitions(n, m-1)
exploring different choices.
                                                       return with_m + without_m
```

```
Python object system:
Idea: All bank accounts have a balance and an account holder;
 the Account class should add those attributes to each of its instances
                         >>>> a = Account('Jim')
   A new instance is
                          >>> a.holder
 created by calling a
                          'Jim'
         class
                          >>> a.balance
                                                   An account instance
When a class is called:
                                                          holder: 'Jim'
                                             balance: 0
1.A new instance of that class is created:
2.The __init__ method of the class is called with the new object as its first
  argument (named self), along with any additional arguments provided in the
  call expression.
                      class Account:
                         >def __init__(self, account_holder):
   init is called a
                              self.balance = 0
      constructor
                              self.holder = account_holder
                          def deposit(self, amount):
                              self.balance = self.balance + amount
                              return self.balance
  self should always be
                              withdraw(self, amount):
if amount > self.balance:
    return 'Insufficient funds'
                          def
 bound to an instance of
 the Account class or a
   subclass of Account
                              self.balance = self.balance - amount
                              return self.balance
                       >>> type(Account.deposit)
  Function call: all
                       <class 'function'
                       >>> type(a.deposit)
  arguments within
     parentheses
                       <class 'method':
                       >>> Account.deposit(a, 5)
  Method invocation:
  One object before
  the dot and other
                           a.deposit(2)
                                                   Call expression
                       12
   arguments within
     parentheses
                            Dot expression
                           <expression> . <name>
 The <expression> can be any valid Python expression.
 The <name> must be a simple name.
 Evaluates to the value of the attribute looked up by <name> in the object
 that is the value of the <expression>.
 To evaluate a dot expression:
 1. Evaluate the <expression> to the left of the dot, which yields
     the object of the dot expression
     <name> is matched against the instance attributes of that object;
     if an attribute with that name exists, its value is returned
    If not, <name> is looked up in the class, which yields a class
     attribute value
     That value is returned unless it is a function, in which case a
     bound method is returned instead
```

Assignment statements with a dot expression on their left-hand side affect attributes for the object of that dot expression

• If the object is an instance, then assignment sets an instance attribute

• If the object is a class, then assignment sets a class attribute

```
Account class
                             interest: 0.02 0.04 0.05
           attributes
                             (withdraw, deposit, _
                                                   init
                                                        balance:
    Instance
                   balance:
                             0
                                         Instance
                              'Jim'
                                                                   'Tom'
                   holder:
                                                        holder:
 attributes of
                                       attributes of
                   interest: 0.08
  jim_account
                                        tom account
                                         >>> jim_account.interest = 0.08
>>> jim_account = Account('Jim')
    tom_account = Account('Tom')
                                         >>> jim_account.interest
                                         0.08
>>> tom_account.interest
0.02
                                         >>> tom account.interest
                                         0.04
>>> jim_account.interest
                                         >>> Account.interest = 0.05
0.02
                                         >>> tom_account.interest
>>> Account.interest = 0.04
                                         0.05
>>> tom_account.interest
                                         >>> jim_account.interest
0.04
                                         0.08
>>> jim_account.interest
0.04
```

To look up a name in a class:

1. If it names an attribute in the class, return the attribute value.

```
2. Otherwise, look up the name in the base class, if there is one.
>>> ch = CheckingAccount('Tom') # Calls Account.__init__
>>> ch.interest # Found in CheckingAccount
0.01
>>> ch.deposit(20) # Found in Account
20
>>> ch.withdraw(5) # Found in CheckingAccount
```