

Environments

Announcements

Environments for Higher-Order Functions

Names can be Bound to Functional Arguments

```
1 def apply_twice(f, x):  
2     return f(f(x))  
3  
→ 4 def square(x):  
5     return x * x  
6  
→ 7 result = apply_twice(square, 2)
```

Global frame
apply_twice
square

func apply_twice(f, x) [parent=Global]

func square(x) [parent=Global]

Applying a user-defined function:

- Create a new frame
- Bind formal parameters (f & x) to arguments
- Execute the body:
return f(f(x))

```
→ 1 def apply_twice(f, x):  
→ 2     return f(f(x))  
3  
4 def square(x):  
5     return x * x  
6  
7 result = apply_twice(square, 2)
```

2 Global frame

1 f1: apply_twice [parent=Global]

apply_twice
square

func apply_twice(f, x) [parent=Global]

func square(x) [parent=Global]

f
x 2

How to Draw an Environment Diagram

When a function is defined:

Create a function value: `func <name>(<formal parameters>) [parent=<label>]`

Its parent is the current frame.



`f1: make_adder` `func adder(k) [parent=f1]`

Bind `<name>` to the function value in the current frame

When a function is called:

1. Add a local frame, titled with the `<name>` of the function being called.
- ★ 2. Copy the parent of the function to the local frame: `[parent=<label>]`
3. Bind the `<formal parameters>` to the arguments in the local frame.
4. Execute the body of the function in the environment that starts with the local frame.

Currying

Function Currying

```
def make_adder(n):  
    return lambda k: n + k
```

```
>>> make_adder(2)(3)  
5  
>>> add(2, 3)  
5
```

There's a general
relationship between
these functions

(Demo)

Curry: Transform a multi-argument function into a single-argument, higher-order function

Environment Diagram Practice

Fall 2022 CS 61A Midterm 1, Question 2

- The Diagram
- Annotations

```

1: def f(x):
2:     """f(x)(t) returns max(x*x, 3*x)
3:     if t(x) > 0, and 0 otherwise.
4:     """
5:     y = max(x * x, 3 * x)
6:     def zero(t):
7:         if t(x) > 0:
8:             return y
9:         return 0
10:    return zero
11:
12: # Find the largest positive y below 10
13: # for which f(y)(lambda z: z - y + 10)
14: # is not 0.
15: y = 1
16: while y < 10:
17:     if f(y)(lambda z: z - y + 10):
18:         max = y
19:     y = y + 1
    
```

