

Computational Structures in Data Science



Recursion



UC Berkeley | Computer Science 88 | Michael Ball | https://cs88.org

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Announcements

- Maps is out
 - Checkpoint 1 is due tonight. It's a few short functions
 - No slip days for the check point, but slip days for the rest of the project.
- Midterm:
 - Thursday 3/11
 - Includes recursion (today and Friday)



Computing In The News

Al Can Write a Passing College Paper in 20 Minutes
 ZDNet Greg Nichols February 24, 2021

Researchers at Education Reference Desk (EduRef), a resource for current and prospective students, found that an artificial intelligence (AI) tool can write a college term paper in three to 20 minutes and achieve a passing grade. Humans, in contrast, took three days on average to complete the same assignment. The researchers had a panel of professors grade anonymous submissions to writing prompts from recent graduates and undergraduatelevel writers and Open AI's GPT-3, a deep learning language prediction model. The professors gave GPT-3 an average grade of "C" in four subjects, and it failed just one assignment. Said the researchers, "Even without being augmented by human interference, GPT-3's assignments received more or less the same feedback as the human writers."



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Computational Structures in Data Science



Recursion



Why Recursion?

- Recursive structures exist (sometimes hidden) in nature and therefore in data!
- It's mentally and sometimes computationally more efficient to process recursive structures using recursion.
- Sometimes, the recursive definition is easier to understand or write, even if it is computationally slower.

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Today: Recursion

re·cur·sion

/riˈkərZHən/ 🌗

noun MATHEMATICS LINGUISTICS

the repeated application of a recursive procedure or definition.

a recursive definition.
 plural noun: recursions

re.cur.sive

/riˈkərsiv/ 🐠

adjective

characterized by recurrence or repetition, in particular.

MATHEMATICS LINGUISTICS

relating to or involving the repeated application of a rule, definition, or procedure to successive results.

COMPUTING

relating to or involving a program or routine of which a part requires the application of the whole, so that its explicit interpretation requires in general many successive executions.

• Recursive function calls itself, directly or indirectly



Demo: Vee

- run 11-recursion.py
- The file will open an interpreter.
- Use the following keys to play with the demo
 - Space to draw
 - C to Clear
 - Up to add "vee" to the functions list
 - Down to remove the "vee" functions from the list.



Demo: Countdown

```
def countdown(n):
    if n == 0:
        print('Blastoff!')
    else:
        print(n)
        countdown(n - 1)
```



The Recursive Process

- Recursive solutions involve two major parts:
 - Base case(s), the problem is simple enough to be solved directly
 - Recursive case(s). A recursive case has three components:
 - Divide the problem into one or more simpler or smaller parts
 - Invoke the function (recursively) on each part, and
 - Combine the solutions of the parts into a solution for the problem.



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Learning Objectives

- Compare Recursion and Iteration to each other
 - Translate some simple functions from one method to another
- Write a recursive function
 - Understand the base case and a recursive case



Iteration vs Recursion: Sum Numbers

For loop: def sum(n): s=0 for i in range(0,n+1): s=s+i return s



Iteration vs Recursion: Sum Numbers

While loop: def sum(n): s=0 i=0 while i<n: i=i+1 s=s+i return s



Iteration vs Recursion: Sum Numbers

Recursion: def sum(n): if n == 0: return 0 return n+sum(n-1)



Iteration vs Recursion: Cheating!

Sometimes it's best to just use a formula! But that's not always the point. igodot

def sum(n): return (n * (n + 1)) / 2



The Recursive Process

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Recall: Iteration







Recursion Key concepts – by example





In words

- The sum of no numbers is zero
- The sum of 1^2 through n^2 is the
 - sum of 1^2 through $(n-1)^2$
 - plus n²

```
def sum_of_squares(n):
    if n < 1:
        return 0
    else:
        return sum_of_squares(n-1) + n**2</pre>
```



Why does it work

```
sum_of_squares(3)
# sum_of_squares(3) => sum_of_squares(2) + 3**2
# => sum_of_squares(1) + 2**2 + 3**2
# => sum_of_squares(0) + 1**2 + 2**2 + 3**2
# => 0 + 1**2 + 2**2 + 3**2 = 14
```



Review: Functions



- Generalizes an expression or set of statements to apply to lots of instances of the problem
- A function should *do one thing well*



How does it work?

- Each recursive call gets its own local variables
 - Just like any other function call
- Computes its result (possibly using additional calls)
 - Just like any other function call
- Returns its result and returns control to its caller
 - Just like any other function call
- The function that is called happens to be itself
 - Called on a simpler problem
 - Eventually stops on the simple base case



Questions

- In what order do we sum the squares ?
- How does this compare to iterative approach ?

```
def sum_of_squares(n):
    accum = 0
    for i in range(1,n+1):
        accum = accum + i*i
    return accum
```

<pre>def sum_of_squares(n):</pre>	<pre>def sum_of_squares(n):</pre>
if n < 1:	if n < 1:
return 0	return 0
else:	else:
return sum_of_squares(n-1) + n**2	return n**2 + sum_of_squares(n-1)



Trust ...

• The recursive "leap of faith" works as long as we hit the base case eventually

What happens if we don't?



Why Recursion?

- "After Abstraction, Recursion is probably the 2nd biggest idea in this course"
- "It's tremendously useful when the problem is self-similar"
- "It's no more powerful than iteration, but often leads to more concise & better code"
- "It's more 'mathematical""
- "It embodies the beauty and joy of computing"
- ...



Recursion (unwanted)



Example I

List all items on your hard disk







Another Example



• Recursion over sequence length, rather than number magnitude

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Why Recursion? More Reasons

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