HIGHER ORDER FUNCTIONS AND ENVIRONMENT DIAGRAMS

Computer Science 88

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1 Higher Order Functions

A **higher order function** (HOF) is a function that manipulates other functions by taking in functions as arguments, returning a function, or both.

1.1 Functions as Arguments

One way a higher order function can exploit other functions is by taking functions as input. Consider this higher order function called negate.

```
def negate(f, x):
    return -f(x)
```

negate takes in a function f and a number x. It doesn't care what exactly f does, as long as f takes in a number and returns a number. Its job is simple: call f on x and return the negation of that value.

1.2 Questions

1. Here are some possible functions that can be passed through as f.

```
def square(n):
    return n * n
```

```
def double(n):
    return 2 * n
```

What will the following Python statements output? >>> negate(square, 5)

Solution:

-25

```
>>> negate(double, -19)
```

Solution:

38

```
>>> negate(double, negate(square, -4))
```

Solution: 32

2. Implement a function keep_ints, which takes in a function cond and a number n, and only prints a number from 1 to n if calling cond on that number returns True: def keep_ints(cond, n):

```
"""Print out all integers 1..i..n where cond(i) is true
>>> def is_even(x):
... # Even numbers have remainder 0 when divided by 2.
... return x % 2 == 0
>>> keep_ints(is_even, 5)
2
4
"""
```

Solution: i = 1 while i <= n:</pre>

```
if cond(i):
    print(i)
i += 1
```

1.3 Functions as Return Values

Often, we will need to write a function that returns another function. One way to do this is to define a function inside of a function:

```
def outer(x):
    def inner(y):
        ...
    return inner
```

The return value of outer is the function inner. This is a case of a function returning a function. In this example, inner is defined inside of outer. Although this is a common pattern, we can also define inner outside of outer and still use the same return statement.

```
def inner(y):
    ...
def outer(x):
    return inner
```

1.4 Questions

1. Use this definition of outer to fill in what Python would print when the following lines are evaluated.

```
def outer(n):
    def inner(m):
        return n - m
    return inner
>>> outer(61)
```

```
Solution:
```

```
<function outer.inner ...>
```

```
>>> f = outer(10)
>>> f(4)
```

Solution:

6

>>> outer(5)(4)

Solution: 1

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```
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```

2. Implement a function keep_ints like before, but now it takes in a number n and returns a function that has one parameter cond. The returned function prints out all numbers from 1..i..n where calling cond(i) returns True.

```
def keep_ints(n):
    """Returns a function which takes one parameter cond and
    prints out all integers 1..i..n where calling cond(i)
    returns True.
    >>> def is_even(x):
    ...    # Even numbers have remainder 0 when divided by 2.
    ...    return x % 2 == 0
    >>> keep_ints(5)(is_even)
    2
    4
    """
```

Solution:

```
def do_keep(cond):
    i = 1
    while i <= n:
        if cond(i):
            print(i)
            i += 1
return do_keep</pre>
```

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2 Environment

3 Questions

Draw the environment diagram for evaluating the following code def f(x):

```
return y + x
y = 10
f(8)
```

Solution: Solution: https://goo.gl/rZnzaM

2. Draw the environment diagram for evaluating the following code

Solution: Solution: https://goo.gl/4m3NRD

3. Draw the environment diagram for evaluating the following code

```
def foo(x, y):
    foo = bar
    return foo(bar(x, x), y)
def bar(z, x):
    return z + y

y = 5
foo(1, 2)
```

Solution: Solution: https://goo.gl/7Kcx6n

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```
4. Draw the environment diagram for evaluating the following code def spain(japan, iran):
    def world(cup, egypt):
        return japan-poland
    return iran(world(iran, poland))
    def saudi(arabia):
        return japan + 3
    japan, poland = 3, 7
    spain(poland+1, saudi)
```

Solution: Solution: https://goo.gl/iddW49

```
5. Draw the environment diagram for evaluating the following code
  cap = 9
  hulk = 3
  def marvel(cap, thor, avengers):
      marvel = avengers
      iron = hulk + cap
      if thor > cap:
           def marvel(cap, thor, avengers):
               return iron
      else:
           iron = hulk
      return marvel(thor, cap, marvel)
  def iron(man):
      hulk = cap - 1
      return hulk
  marvel(cap, iron(3), marvel)
```

Solution: Solution: https://goo.gl/sofcq2