DATA C88C

April 5, 2023

1 Linked Lists

The following is the Link class used to represent linked lists.

```
class Link:
    empty = ()
    def __init__(self, first, rest=empty):
        assert rest is Link.empty or isinstance(rest, Link)
        self.first = first
        self.rest = rest
    def __getitem__(self, i):
        if i == 0:
            return self.first
        return self.rest[i-1]
    def __len__(self):
        return 1 + len(self.rest)
```

We can write lnk.first and lnk.rest to access the first element of the linked list and the rest of the linked list, respectively. In addition to the constructor __init__, we have the special Python methods __getitem__ and __len__. Note that any method that begins and ends with two underscores is a special Python method. Special Python methods may be invoked using built-in functions and special notation. The built-in Python element selection operator, as in lst[i], invokes lst.__getitem__(i). Likewise, the built-in Python function len, as in len(lst), invokes lst.__len__().

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However, we won't use the above special methods in the rest of this worksheet, nor in most of our linked list problems in this class. Instead, we will only use the Link constructor and the self.first and self.rest instance attributes. This will be an exercise in using the recursive structure of linked lists rather than treating them like regular Python lists.

For the rest of this worksheet, assume that you are only given this portion of the Link class implementation:

```
class Link:
    empty = ()
    def __init__(self, first, rest=empty):
        assert rest is Link.empty or isinstance(rest, Link)
        self.first = first
        self.rest = rest
```

2 Questions

1. Write a function that takes in a a linked list and returns the sum of all its elements. You may assume all elements in lnk are integers.

```
def sum_nums(lnk):
    """
    >>> a = Link(1, Link(6, Link(7)))
    >>> sum_nums(a)
    14
    """
```

```
Solution:
```

```
if lnk == Link.empty:
    return 0
return lnk.first + sum_nums(lnk.rest)
```

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2. Write a iterative function is_palindrome that takes a LinkedList, lnk, and returns True if lnk is a palindrome and False otherwise. You can assume you have access to a reverse function that takes a linked list as input and returns a reversed version of the original linked list.

```
def is_palindrome(lnk):
    """
    >>> one_link = Link(1)
    >>> is_palindrome(one_link)
    True
    >>> lnk = Link(1, Link(2, Link(3, Link(2, Link(1)))))
    >>> is_palindrome(lnk)
    True
    >>> is_palindrome(Link(1, Link(2, Link(3, Link(1)))))
    False
    """
```

Solution:

```
reversed = reverse(lnk)
while lnk is not Link.empty and reversed.first == lnk.
first:
    reversed = reversed.rest
    lnk = lnk.rest
return lnk is Link.empty
```

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3. Write a function that takes a sorted linked list of integers and mutates it so that all duplicates are removed.

```
def remove_duplicates(lnk):
    """
    >>> lnk = Link(1, Link(1, Link(1, Link(1, Link(5)))))
    >>> remove_duplicates(lnk)
    >>> lnk
    Link(1, Link(5))
    """
```

Solution: Recursive solution:

```
if lnk is Link.empty or lnk.rest is Link.empty:
    return
if lnk.first == lnk.rest.first:
    lnk.rest = lnk.rest.rest
    remove_duplicates(lnk)
else:
    remove_duplicates(lnk.rest)
```

For a list of one or no items, there are no duplicates to remove.

Now consider two possible cases:

• If there is a duplicate of the first item, we will find that the first and second items in the list will have the same values (that is, lnk.first == lnk.rest.first). We can confidently state this because we were told that the input linked list is in sorted order, so duplicates are adjacent to each other. We'll remove the second item from the list.

Finally, it's tempting to recurse on the remainder of the list (lnk.rest), but remember that there could still be more duplicates of the first item in the rest of the list! So we have to recurse on lnk instead. Remember that we have removed an item from the list, so the list is one element smaller than before. Normally, recursing on the same list wouldn't be a valid subproblem.

• Otherwise, there is no duplicate of the first item. We can safely recurse on the remainder of the list.

```
Iterative solution:
while lnk is not Link.empty and lnk.rest is not Link.
empty:
    if lnk.first == lnk.rest.first:
        lnk.rest = lnk.rest.rest
    else:
        lnk = lnk.rest
```

The loop condition guarantees that we have at least one item left to consider with lnk.

For each item in the linked list, we pause and remove all adjacent items that have the same value. Once we see that lnk.first != lnk.rest.first, we can safely advance to the next item. Once again, this takes advantage of the property that our input linked list is sorted.