

Import statement

1 from math import pi

2 tau = 2 \* pi

Assignment statement

Global frame

Name

pi

Value

3.1416

Binding

Code (left):

Statements and expressions  
Red arrow points to next line.  
Gray arrow points to the line just executed

Frames (right):

A name is bound to a value  
In a frame, there is at most one binding per name

1 from operator import mul

2 def square(x):

3 return mul(x, x)

4 square(-2)

Global frame

mul

square

Intrinsic name of function called

mul

square

Local frame

f1: square [parent=Global]

Formal parameter bound to argument

x

-2

Return value

4

User-defined function

func mul(...) [parent=Global]

func square(x) [parent=Global]

Return value is not a binding!

1 from operator import mul

2 def square(x):

3 return mul(x, x)

4 square(square(3))

Global frame

mul

square

f1: square [parent=Global]

x

3

Return value

9

f2: square [parent=Global]

x

9

Return value

81

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

**Evaluation rule for call expressions:**  
1.Evaluate the operator and operand subexpressions.  
2.Apply the function that is the value of the operator subexpression to the arguments that are the values of the operand subexpressions.

**Applying user-defined functions:**  
1.Create a new local frame with the same parent as the function that was applied.  
2.Bind the arguments to the function's formal parameter names in that frame.  
3.Execute the body of the function in the environment beginning at that frame.

**Execution rule for def statements:**  
1.Create a new function value with the specified name, formal parameters, and function body.  
2.Its parent is the first frame of the current environment.  
3.Bind the name of the function to the function value in the first frame of the current environment.

**Execution rule for assignment statements:**  
1.Evaluate the expression(s) on the right of the equal sign.  
2.Simultaneously bind the names on the left to those values, in the first frame of the current environment.

**Execution rule for conditional statements:**  
Each clause is considered in order.  
1.Evaluate the header's expression.  
2.If it is a true value, execute the suite, then skip the remaining clauses in the statement.

**Evaluation rule for or expressions:**  
1.Evaluate the subexpression <left>.  
2.If the result is a true value v, then the expression evaluates to v.  
3.Otherwise, the expression evaluates to the value of the subexpression <right>.

**Evaluation rule for and expressions:**  
1.Evaluate the subexpression <left>.  
2.If the result is a false value v, then the expression evaluates to v.  
3.Otherwise, the expression evaluates to the value of the subexpression <right>.

**Evaluation rule for not expressions:**  
1.Evaluate <exp>; The value is True if the result is a false value, and False otherwise.

**Execution rule for while statements:**  
1.Evaluate the header's expression.  
2.If it is a true value, execute the (whole) suite, then return to step 1.

208

mul(add(2, mul(4, 6)), add(3, 5))

mul

add(2, mul(4, 6))

add(3, 5)

26

8

add

2

24

3

5

mul

4

6

Dictionary Methods

>>> food = {"ham":10, "cheese":12}  
>>> food["cheese"]  
12  
>>> "peanuts" in food  
False  
>>> food["peanuts"] = 7 # adds key-value pair to food dict  
>>> "peanuts" in food  
True  
>>> food["ham"] = food["ham"] + 1  
>>> food["ham"]  
11  
>>> [(key, food[key]) for key in food]  
[('ham', 11), ('cheese', 12), ('peanuts', 7)]

List comprehensions

[<map exp> for <name> in <iter exp> if <filter exp>]  
Short version: [<map exp> for <name> in <iter exp>]  
A combined expression that evaluates to a list using this evaluation procedure:  
1. Add a new frame with the current frame as its parent  
2. Create an empty *result* list that is the value of the expression  
3. For each element in the iterable value of <iter exp>:  
A. Bind <name> to that element in the new frame from step 1  
B. If <filter exp> evaluates to a true value, then add the value of <map exp> to the result list

List Methods

>>> lst = [8, 61]  
>>> lst.append(10)  
>>> lst  
[8, 61, 10]  
>>> lst.extend([2, 3])  
>>> lst  
[8, 61, 10, 2, 3]  
>>> lst.insert(0, 88)  
>>> lst  
[88, 8, 61, 10, 2, 3]  
>>> lst[1:3]  
[8, 61]  
>>> lst.pop(0)  
88  
>>> lst  
[8, 61, 10, 2, 3]  
>>> lst.remove(61)  
>>> lst  
[8, 10, 2, 3]  
>>> lst.pop()  
3  
>>> lst  
[8, 10, 2]

List Environment Diagram

digits

list

0

1

2

3

1

8

2

8

pairs

list

0

1

10

20

list

0

1

30

40

Lists "Aggregate" Methods

>>> lst = [-2, 4, 6]  
>>> len(lst)  
3  
>>> sum(lst)  
8  
>>> min(lst)  
-2  
>>> max(lst, key=lambda x: -x)  
-2  
>>> lst = [(1, 9), (2, 5), (3, 4)]  
>>> max(lst, key=lambda y: y[0] \* y[1])  
(3, 4)

Executing a for statement:

for <name> in <expression>:  
    <suite>  
1. Evaluate the header <expression>, which must yield an iterable value (a list, tuple, iterator, etc.)  
2. For each element in that sequence, in order:  
A. Bind <name> to that element in the current frame  
B. Execute the <suite>

..., -3, -2, -1, 0, 1, 2, 3, 4, ...

range(-2, 2)

Length: ending value - starting value

Element selection: starting value + index

List constructor

Range with a 0 starting value

Miscellaneous Operations

>>> 5 // 3  
1  
>>> 5 % 3  
2  
>>> 2 \* 3  
6  
>>> 2 + 3  
5  
>>> 6 / 3  
2.0  
>>> min(2, 1, 4, 3)  
1  
>>> max(2, 1, 4, 3)  
4  
>>> abs(-2)  
2  
>>> pow(2, 3)  
8  
>>> len('word')  
4  
>>> print(1, 2)  
1 2

Functional List Operations

goal: transform a list, and return a new result

map(function, list\_of\_inputs)

transform each item by a function.  
function input: 1 argument (each item)  
function output: "anything", a new item  
map output: list of the same length, but possibly new values

filter(function, list\_of\_inputs)

keeps each item where the function is true.  
function input: 1 argument (each item)  
function output: boolean  
filter output: list with possibly fewer items, but values are the same

reduce(function, list\_of\_inputs)

successively combine items.  
function input: 2 arguments (current item, and the previous result)  
function output: type should match the type of each item  
reduce output: usually a "single" item



square = `lambda x,y: x * y`

Evaluates to a function.  
No "return" keyword!

A function  
with formal parameters `x` and `y`  
that returns the value of `"x * y"`

Must be a single expression

`def make_adder(n):`  
Return a function that takes one argument `k` and returns `k + n`.

A function that returns a function

`>>> add_three = make_adder(3)`  
`>>> add_three(4)`  
`7`

The name `add_three` is bound to a function

`def adder(k):`  
return `k + n`  
return `adder`

A local  
def statement

Can refer to names in  
the enclosing function

• Every user-defined **function** has a **parent frame** (often global)

• The parent of a **function** is the frame in which it was **defined**

• Every local **frame** has a **parent frame** (often global)

• The parent of a **frame** is the parent of the function **called**

`1 def make_adder(n):`  
`2 def adder(k):`  
return `k + n`  
`6 add_three = make_adder(3)`  
`7 add_three(4)`

Nested def

3 Global frame  
make\_adder  
add\_three  
f1: make\_adder [parent=G]  
n 3  
adder  
Return value  
f2: adder [parent=f1]  
k 4  
Return value 7

1  
2  
3

A function's signature has all the information to create a local frame

square = `lambda x: x * x`

VS

`def square(x):`  
return `x * x`

• Both create a function with the same domain, range, and behavior.

• Both functions have as their parent the environment in which they were defined.

• Both bind that function to the name `square`.

• Only the `def` statement gives the function an intrinsic name.

When a function is defined:

1. Create a **function value**: `func <name>(<formal parameters>)`

2. Its parent is the current frame.

`f1: make_adder`      `func adder(k) [parent=f1]`

3. Bind `<name>` to the **function value** in the current frame (which is the first frame of the current environment).

When a function is called:

1. Add a **local frame**, titled with the `<name>` of the function being called.

2. Copy the parent of the function to the **local frame**: `[parent=<label>]`

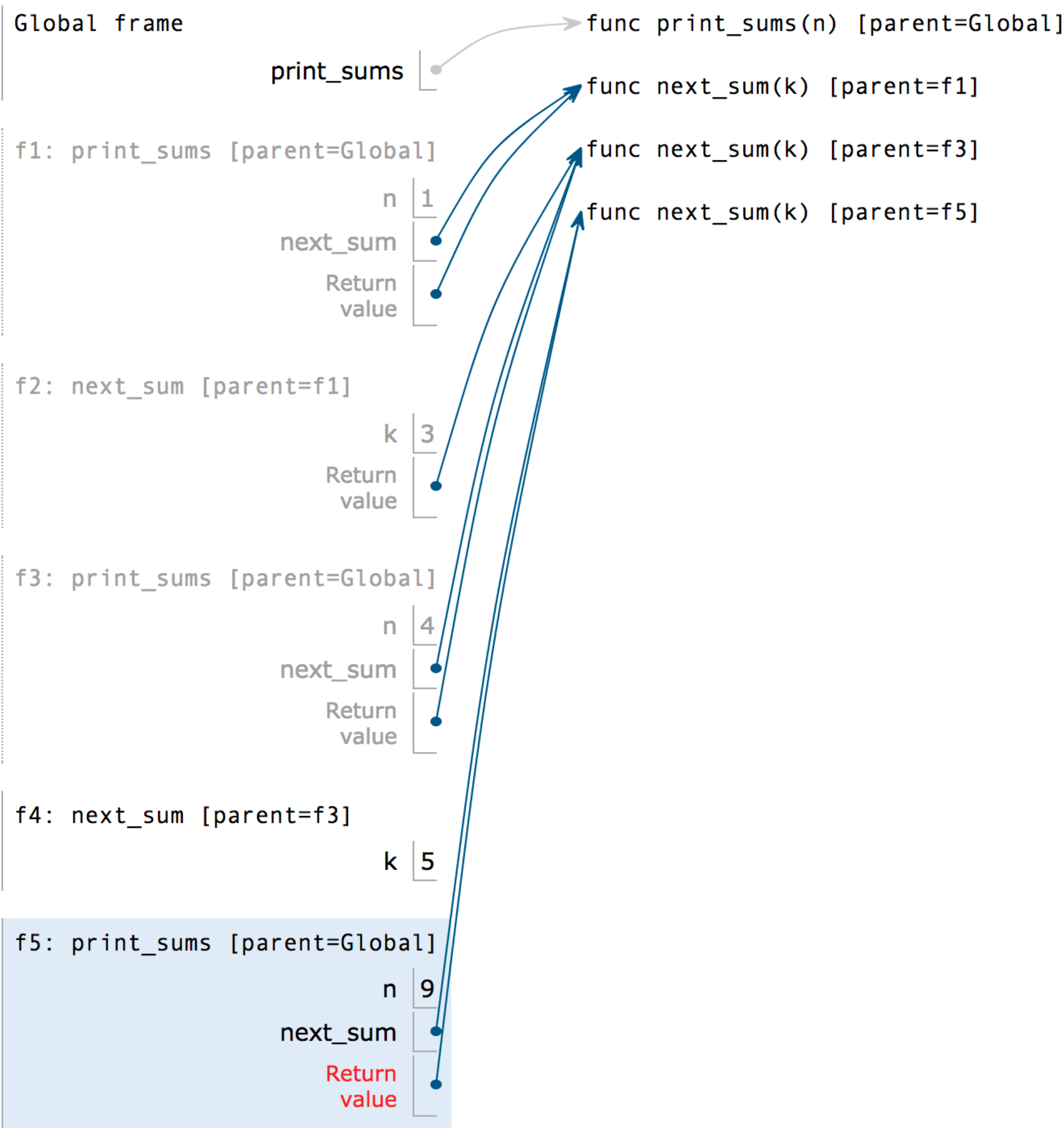
3. Bind the `<formal parameters>` to the arguments in the **local frame**.

4. Execute the body of the function in the environment that starts with the **local frame**.

`1 def print_sums(n):`  
`2 print(n)`  
`3 def next_sum(k):`  
return `print_sums(n+k)`  
`5 return next_sum`  
`6`  
`→ 7 print_sums(1)(3)(5)`

Printed output:

`1`  
`4`  
`9`



Python object system:

**Idea:** All bank accounts have a **balance** and an account **holder**; the **Account** class should add those attributes to each of its instances

`>>> a = Account('Jim')`  
`>>> a.holder`  
`'Jim'`  
`>>> a.balance`  
`0`

A new instance is created by calling a class

An account instance

balance: 0  
holder: 'Jim'

`class Account:`  
def `__init__(self, account_holder):`  
self.balance = 0  
self.holder = account\_holder  
def `deposit(self, amount):`  
self.balance = self.balance + amount  
return self.balance  
def `withdraw(self, amount):`  
if amount > self.balance:  
return 'Insufficient funds'  
self.balance = self.balance - amount  
return self.balance

`__init__` is called a constructor

self should always be bound to an instance of the Account class or a subclass of Account

`>>> type(Account.deposit)`  
`<class 'function'>`  
`>>> type(a.deposit)`  
`<class 'method'>`

Function call:  
all arguments within parentheses

`>>> Account.deposit(a, 5)`  
`10`  
`>>> a.deposit(2)`  
`12`

Method invocation: One object before the dot and other arguments within parentheses

Dot expression

Call expression

False values so far: `0`, `False`, `''`, `None`  
Anything value that's not false is true.

`>>> if 0:`  
... `print('*')`  
`>>> if 1:`  
... `print('*')`  
\*

`>>> if 1 and 0:`  
... `print('*')`  
`>>> if 1 or 0:`  
... `print('*')`  
\*

`>>> if abs:`  
... `print('*')`  
\*

`>>> if 1 or 1/0:`  
... `print('*')`  
\*

`from operator import floordiv, mod`  
def `divide_exact(n, d):`  
Return the quotient and remainder of dividing `N` by `D`.

`>>> q, r = divide_exact(2012, 10)`  
`>>> q`  
`201`  
`>>> r`  
`2`  
return `floordiv(n, d), mod(n, d)`

Multiple assignment to two names

Two return values, separated by commas