# **Functions**

Announcements

#### Announcements

Section 115 is now open.

Everyone(?) on the WL was added to 115.

You must be enrolled in a lab to be enrolled in the course.

Please contact <u>ds-enrollments@berkeley.edu</u> if you need help.

My "Tea Hours": Weds 3:30-4:30pm 784 Soda.

Tea Hours -> advising / general topics, more casual. Encouraged to bring your (legal) beverage of choice.

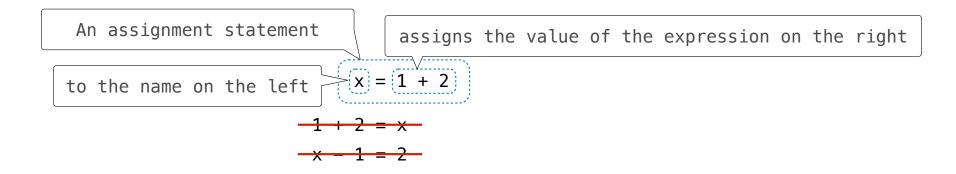
#### This Week:

Lab 0 and Lab 1 due Friday. Normally just 1 lab will be due.

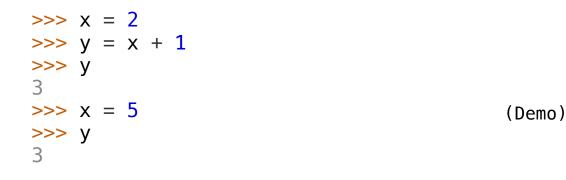
Homework: Released on Tuesday, due the following Wednesday (8 days total)

**Assignment Statements** 

## **Assignment Statements**



The expression (right) is evaluated, and its value is assigned to the name (left).

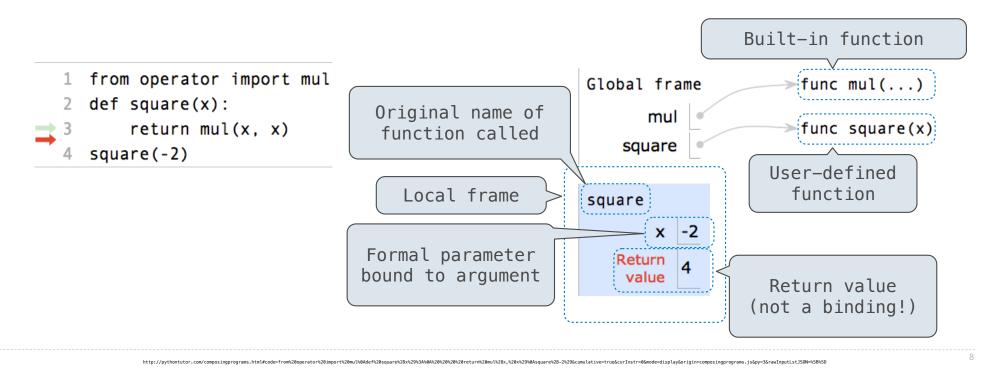


**Environment Diagrams** 

## **Calling User-Defined Functions**

#### Procedure for calling/applying user-defined functions (version 1):

- 1. Add a local frame, forming a new environment
- 2. Bind the function's formal parameters to its arguments in that frame
- 3. Execute the body of the function in that new environment



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### Looking Up Names In Environments

Every expression is evaluated in the context of an environment.

So far, the current environment is either:

- The global frame alone, or
- A local frame, followed by the global frame.

Most important two things I'll say all day:

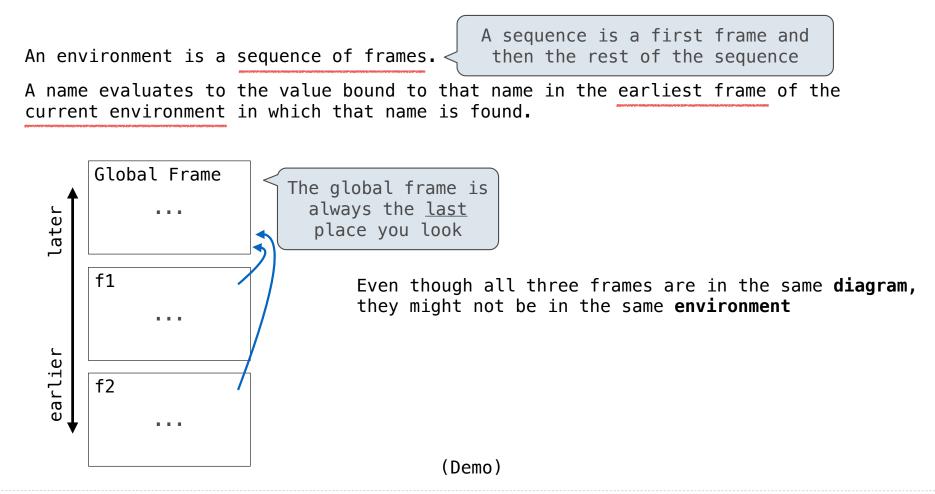
An environment is a sequence of frames.

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

E.g., to look up some name in the body of the square function:

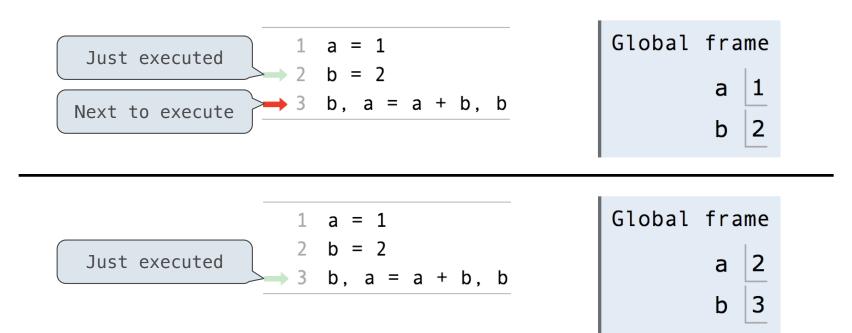
- Look for that name in the local frame.
- If not found, look for it in the global frame.
  (Built-in names like "max" are in the global frame too, but we don't draw them in environment diagrams.)

### A Sequence of Frames



Multiple Assignment

### **Multiple Assignment**



Execution rule for assignment statements:

1. Evaluate all expressions to the right of = from left to right.

http://pvthontutor.com/composingprograms.html#code=a%20%3D%201%0Ab%20%3D%202%0Ab,%20a%20%3D%20a%20%2B%20b,

2. Bind all names to the left of = to those resulting values in the current frame.

(Demo)

ntive=false&curInstr=0&mode=display&origin=composingprograms.is&py=3&rawInputLstJSON=%5B%5

# Print and None

(Demo)

(Optional) Small Expressions

## **Problem Definition**

#### From Discussion 0:

Imagine you can call only the following three functions:

- f(x): Subtracts one from an integer x

- g(x): Doubles an integer x

- h(x, y): Concatenates the digits of two different positive integers x and y. For example, h(789, 12)evaluates to 78912 and h(12, 789) evaluates to 12789.

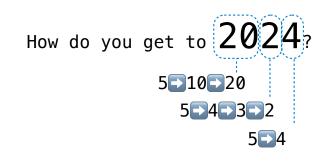
**Definition:** A small expression is a call expression that contains only f, g, h, the number 5, and parentheses. All of these can be repeated. For example, h(g(5), f(f(5))) is a small expression that evaluates to 103.

What's the shortest small expression you can find that evaluates to 2024?	
evaluates to 2024?	Fewest calls? Shortest length when written?

#### A Simple Restatement:

You start with 5. You can:

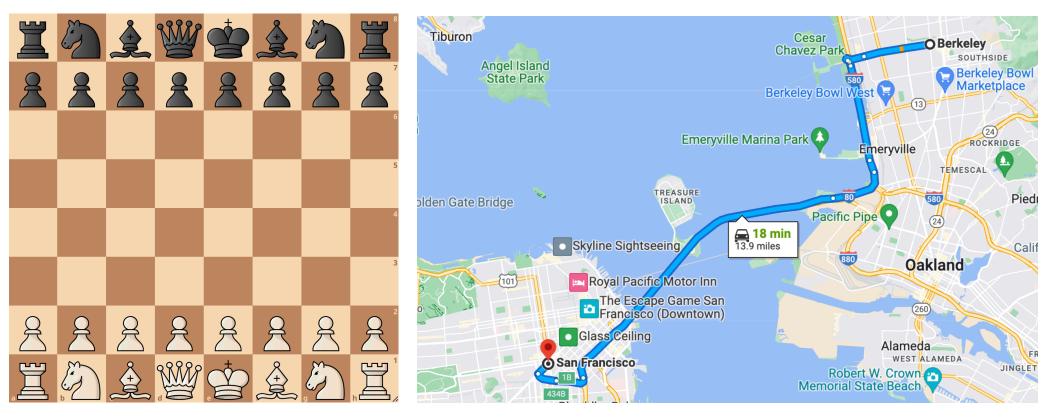
- Subtract 1 from a number
- Double a number
- Glue two numbers together



#### Effective problem solving:

- Understand the problem
- Come up with ideas
- Turn those ideas into solutions

# Search



A common strategy: try a bunch of options to see which is best

Computer programs can evaluate many alternatives by repeating simple operations

#### A Computational Approach

Try all the small expressions with 3 function calls, then 4 calls, then 5 calls, etc.  $f(f(f(5))) \rightarrow 2$ f(f(h(5,5))) -> 53  $h(5,f(f(5))) \rightarrow 53$  $h(q(5), f(5)) \rightarrow 104$  $q(f(f(5))) \rightarrow 6$ q(f(h(5,5))) -> 108 h(5,q(f(5))) -> 58  $h(g(5),g(5)) \rightarrow 1010$ f(q(h(5,5))) -> 109  $f(q(f(5))) \rightarrow 7$  $h(5,f(q(5))) \rightarrow 59$ h(g(5),h(5,5)) -> 1055 g(g(h(5,5))) -> 220 h(5,g(g(5))) -> 520  $q(q(f(5))) \rightarrow 16$  $h(h(5,5),f(5)) \rightarrow 554$ h(h(5,5),g(5)) -> 5510 f(f(g(5))) -> 8 f(h(5,f(5))) -> 53  $h(5,f(h(5,5))) \rightarrow 554$  $q(f(q(5))) \rightarrow 18$ q(h(5,f(5))) -> 108 h(5,g(h(5,5))) -> 5110 h(h(5,5),h(5,5)) -> 5555 f(q(q(5))) -> 19 f(h(5,q(5))) -> 509 h(5,h(5,f(5))) -> 554 h(f(f(5)),5) -> 35  $q(q(q(5))) \rightarrow 40$ q(h(5,q(5))) -> 1020 h(5,h(5,q(5))) -> 5510 h(q(f(5)),5) -> 85 f(h(5,h(5,5))) -> 554 h(5,h(5,h(5,5))) -> 5555 h(f(q(5)),5) -> 95 q(h(5,h(5,5))) -> 1110 h(5,h(f(5),5)) -> 545  $h(q(q(5)), 5) \rightarrow 205$ f(h(f(5),5)) -> 44 h(5,h(q(5),5)) -> 5105 h(f(h(5,5)),5) -> 545  $q(h(f(5),5)) \rightarrow 90$ h(5,h(h(5,5),5)) -> 5555 h(q(h(5,5)),5) -> 1105  $f(h(q(5),5)) \rightarrow 104$  $h(f(5), f(5)) \rightarrow 44$ h(h(5,f(5)),5) -> 545  $q(h(q(5),5)) \rightarrow 210$  $h(f(5),q(5)) \rightarrow 410$ h(h(5,q(5)),5) -> 5105 f(h(h(5,5),5)) -> 554 h(h(5,h(5,5)),5) -> 5555 h(f(5),h(5,5)) -> 455  $q(h(h(5,5),5)) \rightarrow 1110$ h(h(f(5),5),5) -> 455 h(h(q(5),5),5) -> 1055 h(h(h(5,5),5),5) -> 5555 **Reminder:** f(x) subtracts 1; g(x) doubles; h(x, y) concatenates

A Computational Approach

Try all the small expressions with 3 function calls, then 4 calls, then 5 calls, etc.

g(h(g(5),g(g(f(f(5)))))) -> 2024 has 7 calls and 24 characters. g(g(f(f(f(h(5,g(5))))))) -> 2024 has 8 calls and 27 characters. g(h(g(5),g(f(f(g(f(5))))))) -> 2024 has 8 calls and 29 characters. f(h(g(g(5)),h(f(f(f(5))),5))) -> 2024 has 8 calls and 29 characters. f(h(f(f(h(g(g(5)),f(5)))),5)) -> 2024 has 8 calls and 29 characters. f(h(f(f(h(g(g(5)),f(5)))),5)) -> 2024 has 8 calls and 29 characters. f(h(f(h(g(g(5)),f(f(5)))),5)) -> 2024 has 8 calls and 29 characters. f(h(f(h(g(g(5)),f(f(f(5)))),5)) -> 2024 has 8 calls and 29 characters. f(h(h(g(g(5)),f(f(f(5)))),5)) -> 2024 has 8 calls and 29 characters. h(g(g(5)),g(g(g(f(f(5)))),5)) -> 2024 has 8 calls and 29 characters. h(g(g(5)),f(h(f(f(f(5))),5))) -> 2024 has 8 calls and 29 characters. h(g(g(5)),f(h(f(f(f(5))),f(5))) -> 2024 has 8 calls and 29 characters. h(g(g(5)),h(f(f(f(5))),f(5))) -> 2024 has 8 calls and 29 characters. h(f(f(h(g(g(5)),5)))),f(5)) -> 2024 has 8 calls and 29 characters. h(f(f(h(g(g(5)),f(f(5)))),f(5)) -> 2024 has 8 calls and 29 characters. h(f(f(h(g(g(5)),f(f(5)))),f(5)) -> 2024 has 8 calls and 29 characters. h(f(f(h(g(g(5)),f(f(5)))),f(5)) -> 2024 has 8 calls and 29 characters. h(f(f(h(g(g(5)),f(f(5)))),f(5)) -> 2024 has 8 calls and 29 characters. h(f(f(h(g(g(5)),f(f(5)))),f(5)) -> 2024 has 8 calls and 29 characters. h(f(h(g(g(5)),f(f(5)))),f(5)) -> 2024 has 8 calls and 29 characters. h(f(h(g(g(5)),f(f(5)))),f(5)) -> 2024 has 8 calls and 29 characters. h(f(h(g(g(5)),f(f(5)))),f(5)) -> 2024 has 8 calls and 29 characters.

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