

Recursion

Announcements

Countdown

```
def countdown(n):  
    if n == 0:  
        print('Blastoff!')  
    else:  
        print(n)  
        countdown(n-1)
```

```
countdown(10)
```

```
# What's different here?  
def countdown(n):  
    if n == 0:  
        print('Blastoff!')  
    else:  
        countdown(n-1)  
        print(n)
```

```
countdown(10)
```

Recursive Process

- 1: **Divide** – Break the problem down into smaller parts.
- 2: **Invoke** – Make the actual recursive call.
- 3: **Combine** – Use the result of the recursive call in your result.

```
def fact(n):  
    """Compute n factorial.  
  
>>> fact(5)  
120  
>>> fact(0)  
1  
"""  
    if n == 0 or n == 1:  
        return 1  
    else:  
        return fact(n-1) * n
```

Discussion Question: Factorial Two Ways

Rewrite `fact(n)` so that the result of `fact(5)` is computed using the following steps:

```
5 (1 * 5)
20 (1 * 5 * 4)
60 (1 * 5 * 4 * 3)
120 (1 * 5 * 4 * 3 * 2)
```

```
def fact(n):
    """Compute n factorial.

    >>> fact(5)
    120
    >>> fact(0)
    1
    """
    if n == 0 or n == 1:
        return 1
    else:
        return fact(n-1) * n
```

Recursion Visualizer

<https://recursionvisualizer.com>

[View fact\(10\)](#)

```
def fact(n):  
    """Compute n factorial.  
  
    >>> fact(5)  
    120  
    >>> fact(0)  
    1  
    """  
    if n == 0 or n == 1:  
        return 1  
    else:  
        return fact(n-1) * n
```

[View fact\(10\)](#)
~~[View fact\(10\)](#)~~

Tracing Functions

```
from ucb import trace # download ucb.py
```

```
@trace
def fact(n):
    if n == 0 or n == 1:
        return 1
    else:
        return fact(n-1) * n
```

```
# or
```

```
fact = trace(fact)
```


Discussion Question: Play Twenty-One

Rewrite play as a recursive function without a while statement.

- Do you need to define a new inner function? Why or why not? If so, what are its arguments?
- What is the base case and what is returned for the base case?

```
def play(strategy0, strategy1, goal=21):  
    """Play twenty-one and return the winner.
```

```
>>> play(two_strat, two_strat)
```

```
1
```

```
.....
```

```
n = 0
```

```
who = 0 # Player 0 goes first
```

```
while n < goal:
```

```
    if who == 0:
```

```
        n = n + strategy0(n)
```

```
        who = 1
```

```
    elif who == 1:
```

```
        n = n + strategy1(n)
```

```
        who = 0
```

```
return who
```

```
def play(strategy0, strategy1, goal=21):  
    """Play twenty-one and return the winner.
```

```
>>> play(two_strat, two_strat)
```

```
1
```

```
.....
```

```
def f(n, who):
```

```
    if n >= goal:
```

```
        return who
```

```
    if who == 0:
```

```
        n = n + strategy0(n)
```

```
        who = 1
```

```
    elif who == 1:
```

```
        n = n + strategy1(n)
```

```
        who = 0
```

```
    return f(n, who)
```

```
return f(0, 0)
```