

## Designing Functions

---

## Announcements

SQL

## Conceptual Order of Execution

---

## SQL simple “Order of Execution”

<b>SELECT</b> S	<b>3</b>
<b>FROM</b> R1, R2, ...	<b>1</b>
<b>WHERE</b> C1	<b>2</b>

A **SELECT FROM WHERE (SFW)** query is the most standard SQL query structure that extract records from a relation.

Order of execution:

1. **FROM**: Fetch the tables and compute the cross product of R1, R2, ...
2. **WHERE**: “Row filter.” For each tuple from step 1, keep only those that satisfy condition C1
3. **SELECT**: add to output based on S

## “SFW” Examples

<b>SELECT S</b>	<b>3</b>
<b>FROM R1, R2, ...</b>	<b>1</b>
<b>WHERE C1</b>	<b>2</b>

A **SELECT FROM WHERE (SFW)** query is the most standard SQL query structure that extract records from a relation.

```
SELECT flavor, price,  
price * 2 as tariff_price  
FROM cones;
```

Select some columns, possibly apply transformations to the data.

```
SELECT *  
FROM cones  
WHERE price > 4;
```

Return just the ice cream cones which have a price > \$4.00

## SQL “Order of Execution”

<b>SELECT</b> S	5	
<b>FROM</b> R1, R2, ...	1	
<b>WHERE</b> C1	2	
<b>GROUP BY</b> A1, A2, ...	3	}
<b>HAVING</b> C2	4	

**Aggregations** happen after filtering.

Order of execution:

1. **FROM**: Fetch the tables and compute the cross product of R1, R2, ...
2. **WHERE**: “Row filter.” For each tuple from step 1, keep only those that satisfy condition C1
3. **GROUP BY**: A1, A2, ...  
For each group, compute all aggregates needed in C2 and S
4. **HAVING**: For each group, check if C2 is satisfied
5. **SELECT**: add to output based on S

## (Review-ish) Python Operations as Data Transformations

---

Function	Action	Input arguments	Input Fn. Returns	Output
<b>map</b>	Transform every item	1 (each item)	"Anything", a new item	<b>List:</b> same length, but possibly new values
<b>filter</b>	Return a list with fewer items	1 (each item)	A Boolean	<b>List:</b> possibly fewer items, values are the same
<b>reduce</b>	"Combine" items together	2 (current item, and the previous result)	Type should match the type each item	A "single" item



## Python Operations as Data Transformations

---

Function	SQL statement	SQL Data	“Parameters”	Output
<b>map</b>	SELECT	values in a row	Functions and column selectors	<b>A row</b> with valued modified, e.g. adding, selecting etc.
<b>filter</b>	WHERE	values in a row	Boolean operations based on columns	<b>The row</b> or possibly no rows.
<b>reduce</b>	GROUP BY	A table, multiple rows	Column selectors — group by matches on equality.	A set of groups.

## Joins Practice

## Returning to Ice Cream Cones

How many dollars (“Total Sales”) did each salesperson sell?

**JOINing on cone id**

**cones:**

id	flavor	color	price
1	strawberry	pink	3.5
2	chocolate	brown	4.75

**sales:**

id	cashier	cone_id
1	Baskin	2
10	Jerry	6

```
SELECT Cashier, SUM(price) AS "Total Sales"
FROM cones c, sales s_
WHERE s.cone_id = c.id
GROUP BY cashier;
```

Cashier	Total Sales
Ben	\$9.75
Jerry	...
Baskin	...

## Discussion Question

---

What's the maximum difference between leg count for two animals with the same weight?

**Approach #1:** Consider all pairs of animals.

```
SELECT MAX(a.legs - b.legs) AS difference
FROM animals AS a, animals AS b
WHERE a.weight = b.weight;
```

**Approach #2:** Group by weight.

```
SELECT MAX(legs) - MIN(legs) AS difference
FROM animals
GROUP BY weight
ORDER BY difference DESC
LIMIT 1;
```

**animals:**

kind	legs	weight
dog	4	20
cat	4	10
ferret	4	10
parrot	2	6
penguin	2	10
t-rex	2	12000

difference
2

## Discussion Question

What are all the kinds of animals that have the maximal number of legs?

```
sqlite> SELECT * FROM animals WHERE legs = MAX(legs);  
Parse error: misuse of aggregate function MAX()
```

**Approach #1:** Give the maximum number of legs a name.

```
CREATE TABLE m AS SELECT MAX(legs) AS max_legs FROM animals;  
SELECT kind FROM animals, m WHERE legs = max_legs;
```

**animals:**

kind	legs	weight
dog	4	20
cat	4	10
ferret	4	10
parrot	2	6
penguin	2	10
t-rex	2	12000

**Approach #2:** For each kind of animal, compare its legs to the maximum legs by grouping.

```
SELECT a.kind FROM animals AS a, animals AS b GROUP BY a.kind HAVING a.legs = MAX(b.legs);
```

## Implementing Functions

## A Slight Variant of Fall 2022 Midterm 1 3(b)

Implement `nearest_prime`, which takes an integer `n` above 5. It returns the nearest prime number to `n`. If two prime numbers are equally close to `n`, return the larger one. Assume `is_prime(n)` is implemented already.

```
def nearest_prime(n):    Example: n is 21
    """Return the nearest prime number to n.
    In a tie, return the larger one.
```

```
>>> nearest_prime(8)
7
>>> nearest_prime(11)
11
>>> nearest_prime(21)
23
"""
```

```
k = 0
while True:
    if is_prime(23) :
        return 23
    if            :
        k = -k
    else:
        k =           
```

*keep looking for a prime*

### From discussion:

Describe a process (in English) that computes the output from the input using simple steps.

Figure out what additional names you'll need to carry out this process.

Implement the process in code using those additional names.

Read the description

Verify the examples & pick a simple one

Read the template

Annotate names with values from your chosen example

Write code to compute the result

Did you really return the right thing?

Check your solution with the other examples

## A Slight Variant of Fall 2022 Midterm 1 3(b)

Implement `nearest_prime`, which takes an integer `n` above 5. It returns the nearest prime number to `n`. If two prime numbers are equally close to `n`, return the larger one. Assume `is_prime(n)` is implemented already.

```
def nearest_prime(n):    Example: n is 21
    """Return the nearest prime number to n.
    In a tie, return the larger one.
```

```
>>> nearest_prime(8)
```

```
7
```

```
>>> nearest_prime(11)
```

```
11
```

```
>>> nearest_prime(21)
```

```
23
```

```
"""
```

```
k = 0
```

```
while True:
```

```
    if is_prime(n + k): is_prime(23)
```

```
        return n + k    23
```

```
    if k > 0:
```

```
        k = -k
```

```
    else:
```

```
        k = -k + 1
```

*keep  
looking  
for a  
prime*

### From discussion:

Describe a process (in English) that computes the output from the input using simple steps.

Figure out what additional names you'll need to carry out this process.

Implement the process in code using those additional names.

### Process:

*Check whether a number is prime in this order:*

*- original n*

*- n + 1*

*- n - 1*

*- n + 2*

*- n - 2*

*- n + 3*

*- n - 3*

*- n + 4*

*...*

*All of these look like  
n + k for various k*

(Demo)



## Designing Functions

## How to Design Programs

---

### **From Problem Analysis to Data Definitions**

Identify the information that must be represented and how it is represented in the chosen programming language. Formulate data definitions and illustrate them with examples.

### **Signature, Purpose Statement, Header**

State what kind of data the desired function consumes and produces. Formulate a concise answer to the question *what* the function computes. Define a stub that lives up to the signature.

### **Functional Examples**

Work through examples that illustrate the function's purpose.

### **Function Template**

Translate the data definitions into an outline of the function.

### **Function Definition**

Fill in the gaps in the function template. Exploit the purpose statement and the examples.

### **Testing**

Articulate the examples as tests and ensure that the function passes all. Doing so discovers mistakes. Tests also supplement examples in that they help others read and understand the definition when the need arises—and it will arise for any serious program.

## Tree Processing

## Tree-Structured Data

```
class Tree:
    def __init__(self, label, branches=[]):
        self.label = label
        self.branches = list(branches)

    def is_leaf(self):
        return not self.branches
```

A tree can contains other trees:

```
[5, [6, 7], 8, [[9], 10]]
```

```
(+ 5 (- 6 7) 8 (* (- 9) 10))
```

```
(S
  (NP (JJ Short) (NNS cuts))
  (VP (VBP make)
      (NP (JJ long) (NNS delays)))
  (. .))
```

```
<ul>
  <li>Midterm <b>1</b></li>
  <li>Midterm <b>2</b></li>
</ul>
```

Tree processing often involves recursive calls on subtrees

## Designing a Function

Implement `smalls`, which takes a `Tree` instance `t` containing integer labels. It returns the non-leaf nodes in `t` whose labels are smaller than any labels of their descendant nodes.

`def smalls(t):`     *Signature: Tree -> List of Trees*

*"""Return a list of the non-leaf nodes in t that are smaller than all their descendants."""*

>>> a = Tree(1, [Tree(2, [Tree(4), Tree(5)]), Tree(3, [Tree(0, [Tree(6)])])])

>>> sorted([t.label for t in smalls(a)])  
[0, 2]

*"""*

result = []                     *Signature: Tree -> number*

`def process(t):`                *"Find smallest label in t & maybe add t to result"*

*if* t.is\_leaf():

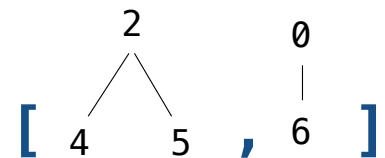
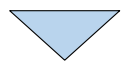
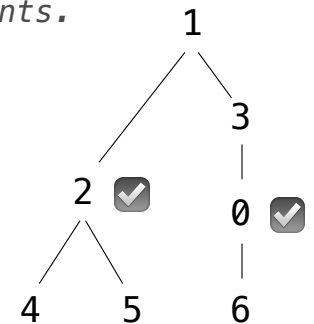
*return* t.label

*else:*

*return* min(...)

process(t)

*return* result



## Designing a Function

Implement `smalls`, which takes a `Tree` instance `t` containing integer labels. It returns the non-leaf nodes in `t` whose labels are smaller than any labels of their descendant nodes.

`def smalls(t):`     *Signature: Tree -> List of Trees*

*"""Return a list of the non-leaf nodes in t that are smaller than all descendants.*

`>>> a = Tree(1, [Tree(2, [Tree(4), Tree(5)]), Tree(3, [Tree(0, [Tree(6)])])])`

`>>> sorted([t.label for t in smalls(a)])`  
`[0, 2]`

*"""*

`result = []`                     *Signature: Tree -> number*

`def process(t):`                *"Find smallest label in t & maybe add t to result"*

*if* `t.is_leaf():`  
          *return* `t.label`

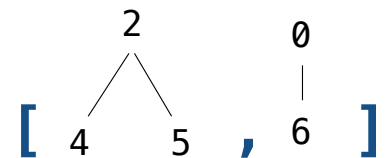
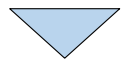
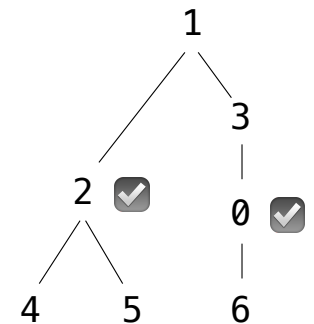
*else:*  
          `smallest = min([process(b) for b in t.branches])`

*if* `t.label < smallest` *:*  
              `result.append( t )`

*return* `min(smallest, t.label)`

`process(t)`

*return* `result`



## Fall 2022 Midterm 2 Question 4(b)

A *hydra* is a Tree with a special structure. Each node has 0 or 2 children. All leaves are heads labeled 1. Each non-leaf body node is labeled with the number of leaves among its descendants.

Implement `chop_head(hydra, n)`, which takes a hydra and a positive integer `n`. It mutates the hydra by replacing the `n`th head from the left with two new adjacent heads & updating all ancestor labels.

```
def chop_head(hydra, n): Signature: (hydra, int) -> None
```

```
    assert n > 0 and n <= hydra.label
```

```
    if hydra.is_leaf():
```

```
        hydra.label = 2
```

```
        hydra.branches = [Tree(1), Tree(1)]
```

```
    else:
```

```
        hydra.label += 1
```

```
        left, right = hydra.branches
```

```
        if n > left.label:
```

```
            chop_head(right, n - left.label)
```

```
        else:
```

```
            chop_head(left, n)
```

*Mutate the hydra*

*Update ancestor*

*nth head*

