# DATA C88C Spring 2025

# Recursion

Many students find this topic challenging. Everything gets easier with practice. Please help each other learn.

## Q1: Swipe

Implement swipe, which prints the digits of argument n, one per line, first backward then forward. The left-most digit is printed only once. Do not use while or for or str. (Use recursion, of course!)

```
def swipe(n):
    """Print the digits of n, one per line, first backward then forward.
    >>> swipe(2837)
    7
    3
    8
    2
    8
    3
    7
    """
    if n < 10:
        print(n)
    else:
        "*** YOUR CODE HERE ***"</pre>
```

First **print** the first line of the output, then make a recursive call, then **print** the last line of the output.

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### Q2: Skip Factorial

Define the base case for the skip\_factorial function, which returns the product of every other positive integer, starting with n.

```
def skip_factorial(n):
    """Return the product of positive integers n * (n - 2) * (n - 4) * ...
    >>> skip_factorial(5) # 5 * 3 * 1
    15
    >>> skip_factorial(8) # 8 * 6 * 4 * 2
    384
    """
    if ___:
        return ___
else:
        return n * skip_factorial(n - 2)
```

If n is even, then the base case will be 2. If n is odd, then the base case will be 1. Try to write a condition that handles both possibilities.

#### Q3: Recursive Hailstone

Recall the hailstone function from Homework 1. First, pick a positive integer n as the start. If n is even, divide it by 2. If n is odd, multiply it by 3 and add 1. Repeat this process until n is 1. Complete this recursive version of hailstone that prints out the values of the sequence and returns the number of steps.

```
def hailstone(n):
    """Print out the hailstone sequence starting at n,
    and return the number of elements in the sequence.
    >>> a = hailstone(10)
    10
    5
    16
    8
    4
    2
    1
    >>> a
    7
    >>> b = hailstone(1)
    1
    >>> b
    1
    .....
    print(n)
    if n % 2 == 0:
        return even(n)
    else:
        return odd(n)
def even(n):
    return ____
def odd(n):
    "*** YOUR CODE HERE ***"
```

An even number is never a base case, so even always makes a recursive call to hailstone and returns one more than the length of the rest of the hailstone sequence.

An odd number might be 1 (the base case) or greater than one (the recursive case). Only the recursive case should call hailstone.

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# Document the Occasion

Please all fill out the attendance form (one submission per person per week).

## Extra Questions

The questions below are optional but recommended if you would like some extra practice.

### Q4: Is Prime

Implement is\_prime that takes an integer n greater than 1. It returns True if n is a prime number and False otherwise. Try following the approach below, but implement it recursively without using a while (or for) statement.

```
def is_prime(n):
    assert n > 1
    i = 2
    while i < n:
        if n % i == 0:
            return False
        i = i + 1
    return True</pre>
```

You will need to define another "helper" function (a function that exists just to help implement this one). Does it matter whether you define it within is\_prime or as a separate function in the global frame? Try to define it to take as few arguments as possible.

```
def is_prime(n):
    """Returns True if n is a prime number and False otherwise.
    >>> is_prime(2)
    True
    >>> is_prime(16)
    False
    >>> is_prime(521)
    True
    """
    "*** YOUR CODE HERE ***"
```

Define an inner function that checks whether some integer between i and n evenly divides n. Then you can call it starting with i=2:

```
def is_prime(n):
    def f(i):
        if n % i == 0:
            return _____
        elif ____:
            return _____
        else:
            return f(____)
        return f(2)
```

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### Q5: Function Repeater

Define a function  $make_fn_repeater$  which takes in a one-argument function f and an integer x. It should return another function which takes in one argument, another integer. This function returns the result of applying f to x this number of times.

Make sure to use recursion in your solution.

```
def make_func_repeater(f, x):
    """
    >>> incr_1 = make_func_repeater(lambda x: x + 1, 1)
    >>> incr_1(2) #same as f(f(x))
    3
    >>> incr_1(5)
    6
    """
    def repeat(______):
        if _____:
        return _____:
        return _____
else:
            return ______
return ______
```