DATA C88C
Summer 2025

Recursion
Discussion 4: July 3, 2025

Recursion

Many students find this topic challenging. Everything gets easier with practice. Please help each other learn.

Q1: Swipe

Implement `swipe`, which prints the digits of argument `n`, one per line, **first backward then forward**. The left-most digit is printed only once. **Do not use `while` or `for` or `str`.** (Use recursion, of course!)

```
def swipe(n):
    """Print the digits of n, one per line, first backward then forward.

    >>> swipe(2837)
    7
    3
    8
    2
    8
    3
    7
    """
    if n < 10:
        print(n)
    else:
        "*** YOUR CODE HERE ***"
```

Q2: Skip Factorial

Define the base case for the `skip_factorial` function, which returns the product of **every other positive integer**, starting with `n`.

```
def skip_factorial(n):
    """Return the product of positive integers n * (n - 2) * (n - 4) * ...

    >>> skip_factorial(5) # 5 * 3 * 1
    15
    >>> skip_factorial(8) # 8 * 6 * 4 * 2
    384
    """
    if ___:
        return ___
    else:
        return ___
```

Q3: Recursive Hailstone

Recall the `hailstone` function from Homework 1. First, pick a positive integer `n` as the start. If `n` is even, divide it by 2. If `n` is odd, multiply it by 3 and add 1. Repeat this process until `n` is 1. Complete this recursive version of `hailstone` that prints out the values of the sequence and returns the number of steps.

```
def hailstone(n):
    """Print out the hailstone sequence starting at n,
    and return the number of elements in the sequence.
    >>> a = hailstone(10)
    10
    5
    16
    8
    4
    2
    1
    >>> a
    7
    >>> b = hailstone(1)
    1
    >>> b
    1
    """
    print(n)
    if n % 2 == 0:
        return even(n)
    else:
        return odd(n)

def even(n):
    return ____

def odd(n):
    "*** YOUR CODE HERE ***"
```

Extra Questions

The questions below are **optional but recommended** if you would like some extra practice.

Q4: Is Prime

Implement `is_prime` that takes an integer `n` greater than 1. It returns `True` if `n` is a prime number and `False` otherwise. Try following the approach below, but implement it recursively without using a `while` (or `for`) statement.

```
def is_prime(n):
    assert n > 1
    i = 2
    while i < n:
        if n % i == 0:
            return False
        i = i + 1
    return True
```

You will need to define another "helper" function (a function that exists just to help implement this one). Does it matter whether you define it within `is_prime` or as a separate function in the global frame? Try to define it to take as few arguments as possible.

```
def is_prime(n):
    """Returns True if n is a prime number and False otherwise.
    >>> is_prime(2)
    True
    >>> is_prime(16)
    False
    >>> is_prime(521)
    True
    """
    "*** YOUR CODE HERE ***"
```

Define an inner function that checks whether some integer between `i` and `n` evenly divides `n`. Then you can call it starting with `i=2`:

```
def is_prime(n):
    def f(i):
        if n % i == 0:
            return ____
        elif ____:
            return ____
        else:
            return f(____)
    return f(2)
```

Q5: Function Repeater

Define a function `make_fn_repeater` which takes in a one-argument function `f` and an integer `x`. It should return another function which takes in one argument, another integer. This function returns the result of applying `f` to `x` this number of times.

Make sure to use recursion in your solution.

```
def make_func_repeater(f, x):
    """
    >>> incr_1 = make_func_repeater(lambda x: x + 1, 1)
    >>> incr_1(2) #same as f(f(x))
    3
    >>> incr_1(5)
    6
    """
    def repeat(__________________):
        if ________________________:
            return __________________
        else:
            return __________________
    return ________________________
```